

# QUANTITATIVE IMAGING, PHYSIOLOGICAL MODELS, AND PERFUSION

DIFFERENCES BETWEEN ANIMAL AND HUMAN STUDIES.  
TECHNICAL ASPECTS OF ANIMAL STUDIES

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# OUTLINE

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1. Quantitative imaging
2. Perfusion imaging (tumor-bearing mice)
3. T1 quantification (rat myocardium)

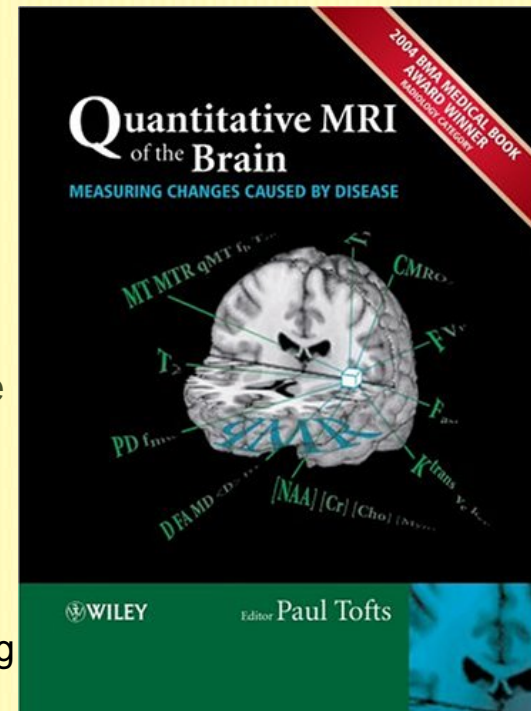
(Differences between animal and human studies.

technical aspects of animal studies)

# 1. QUANTITATIVE IMAGING

## „Quantitative MRI“ (qMRI)

- first in the 1980's – physicists measured the NMR properties of tissue (PD, T1 and T2) – to characterize biological tissue – to differentiate different tissues
- MRI scanner is no **longer a camera**, but a **scientific measuring instrument**
- common (T1w, T2w, PDw, DWI, PWI, ...) images
  - signal intensity in arbitrary units
  - cannot be compared across sites or even scanning sessions
- quantitative imaging
  - biomarkers in physical units (s, mm<sup>2</sup>/s, ml/min/g, ...)
  - absolute measures comparable across imaging sites and time points



1. Tofts PS. Quantitative MRI of the brain: measuring changes caused by disease. John Wiley, 2003.

# 1. QUANTITATIVE IMAGING

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- Proton Density (PD) - water content
- T1, T2 –size of the molecule, tumbling of spins, mobility of  $^1\text{H}$ , water content
- diffusion and its tensor – microscopic details about tissue architecture
- Magnetization transfer – macromolecules (e.g. demyelination in multiple sclerosis)
- spectroscopy – concentrations of metabolites
- dynamic T1-weighted MRI (DCE-MRI) – vessel permeability
- dynamic T2 (\*) - weighted MRI (DCE-MRI) – blood flow and volume
- Arterial Spin Labelling (ASL) – blood flow

## 2. PERFUSION IMAGING

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### Oncology

- tumor characterization
- grading
- treatment monitoring
- pseudo-progression vs. recurrence

### Neurology

- stroke treatment: delay from stroke onset => individualized decision based on the tissue status
- penumbra – salvageable brain tissue, viable brain tissue with reduced perfusion
- based on perfusion and diffusion imaging

## 2. PERFUSION IMAGING

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### Cardiology

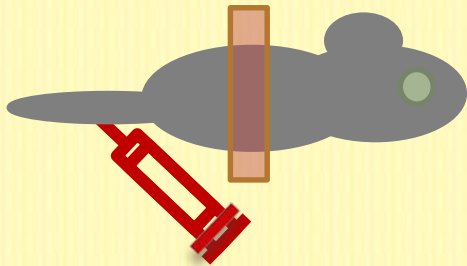
- ischemic diseases – diagnosis
- treatment monitoring

### Preclinical studies

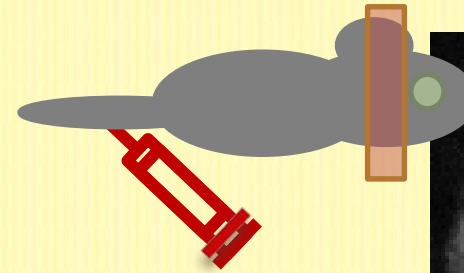
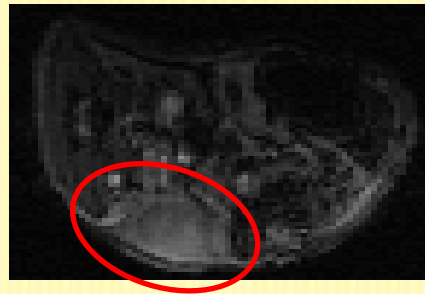
- validation of animal models
- test of BBB opening
- testing of nanoparticle carriers of imaging markers and drugs -> pharmacokinetics, pharmacodynamics
- development of new drugs
- ...

## 2. PERFUSION IMAGING

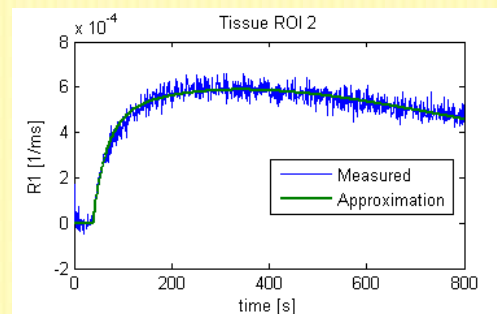
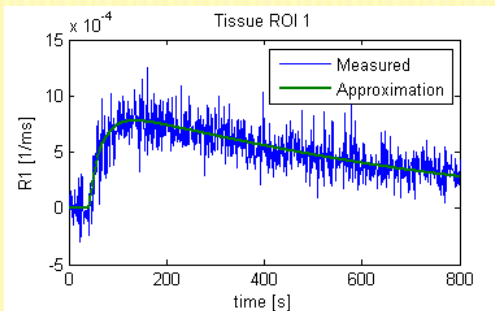
Imaging of contrast-agent distribution in the tissue



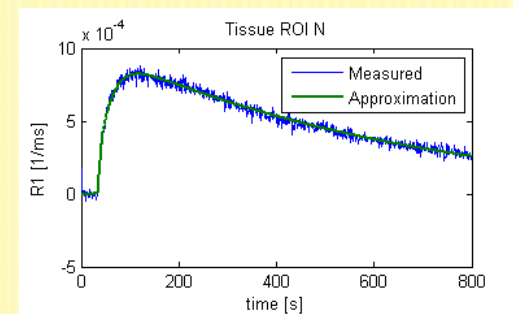
DCE-MRI  
mouse  
subcut. CT26 tumor



DCE-MRI  
rat  
glioblastoma



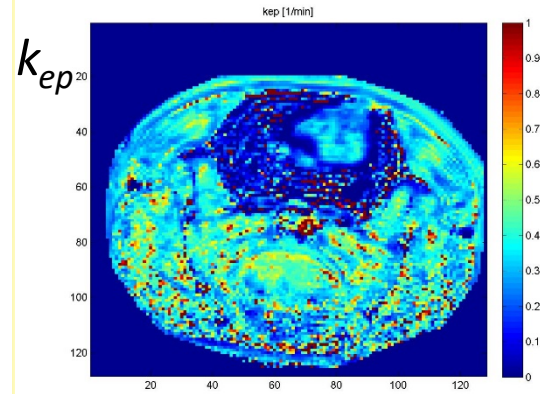
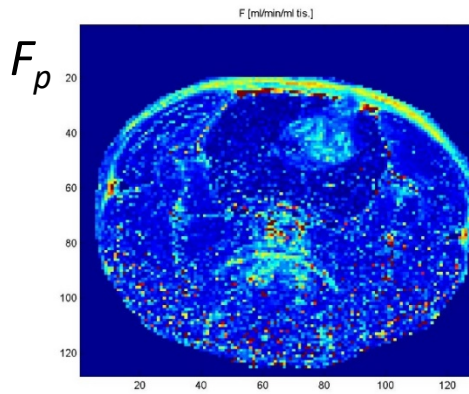
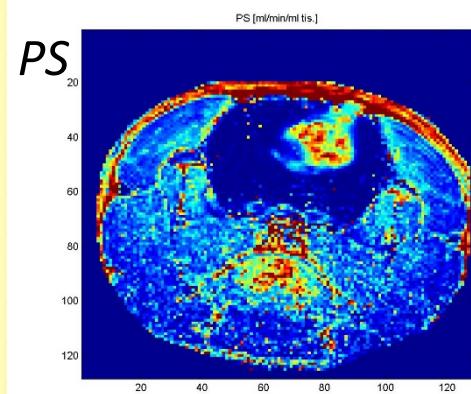
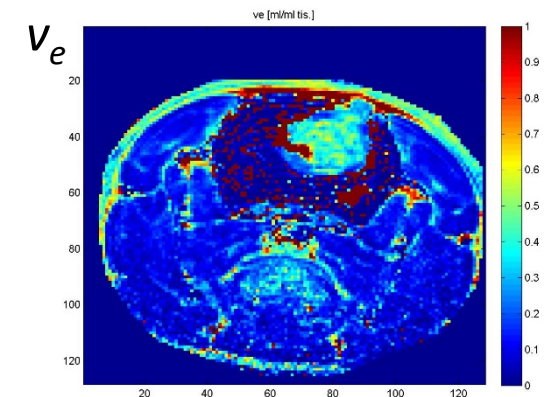
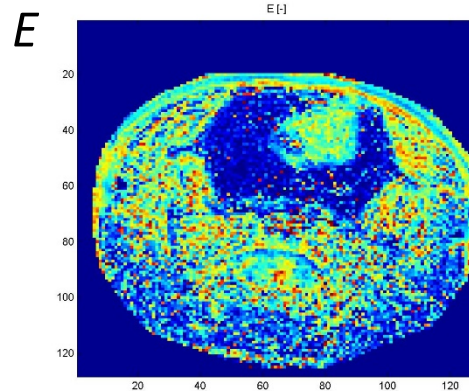
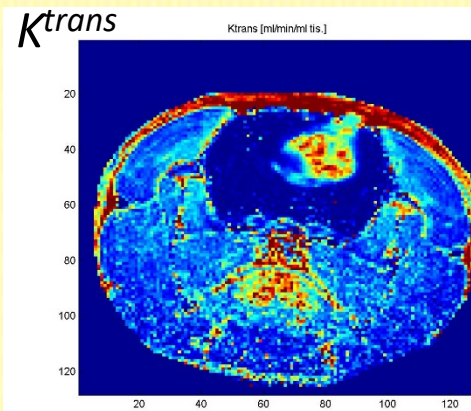
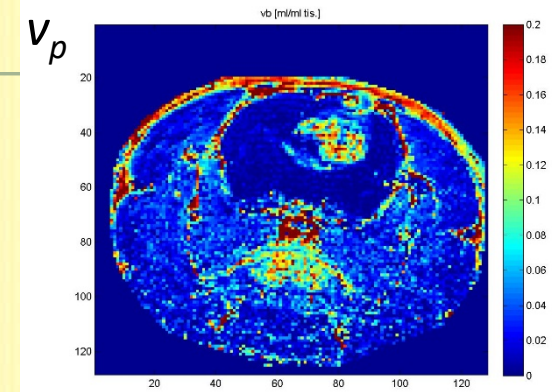
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## 2. PERFUSION IMAGING

### perfusion-parameter maps

- $F_p$  - plasma flow [ml/min/100ml tis.]
- $v_p$  - plasma volume [ml/100 ml tis.]
- $v_e$  - EES volume [ml/100 ml tis.]
- $PS$  - permeability-surface product [ml/min/100ml tis.]
- ...



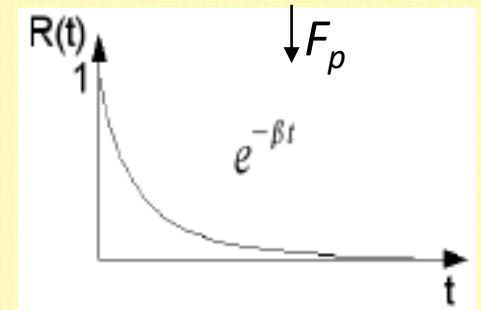
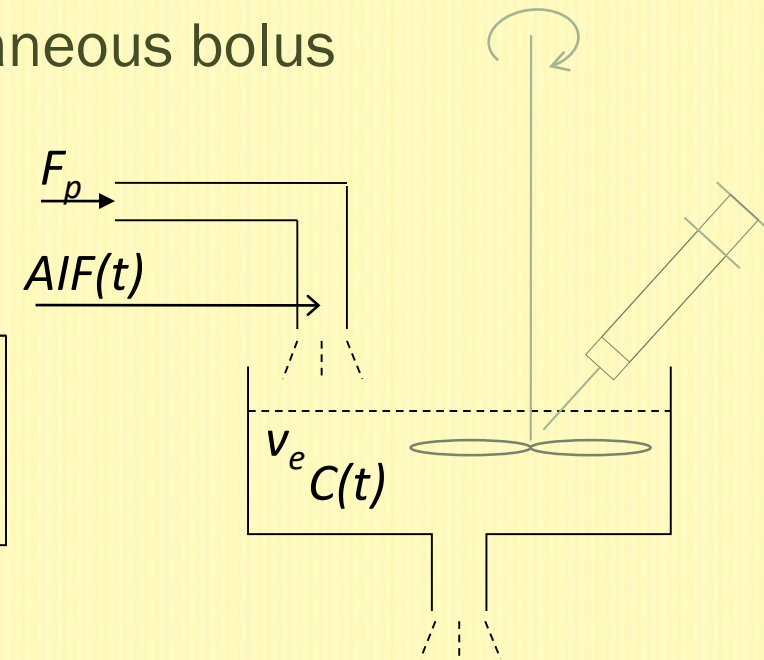
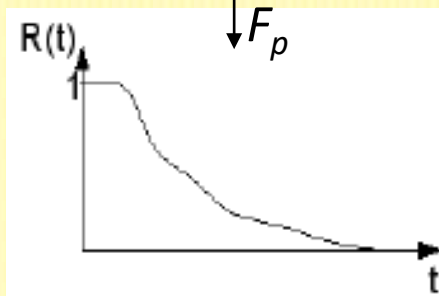
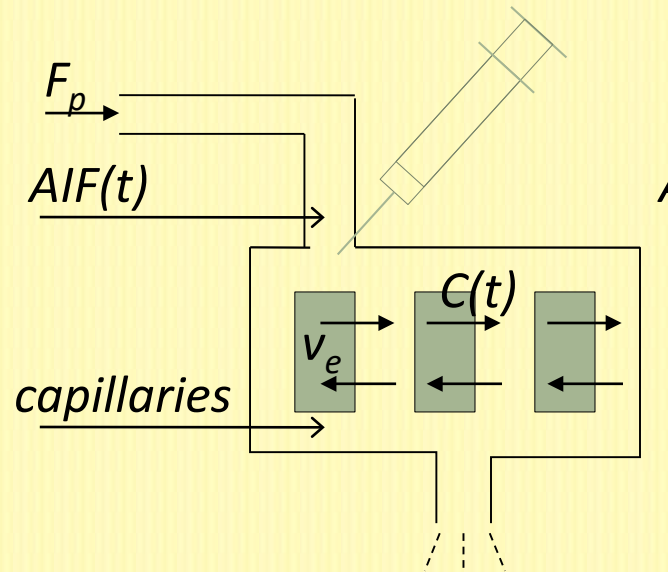
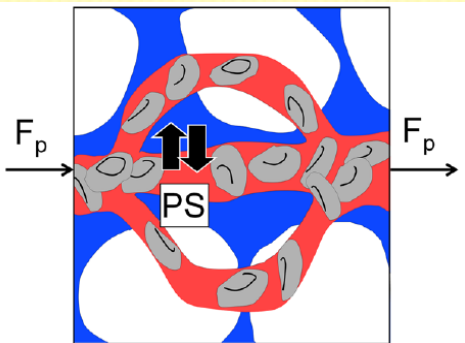


## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

Impulse residual function (IRF) –  $R(t)$

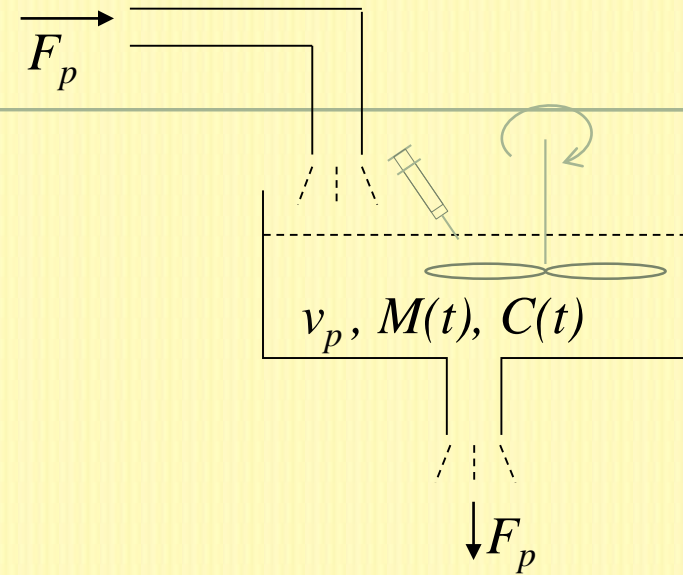
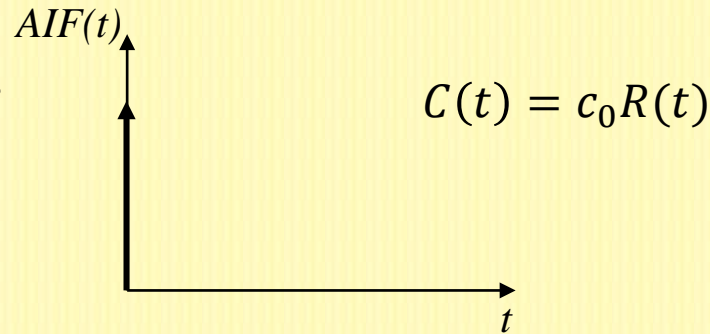
$$C(t) = c_0 R(t)$$

- Characteristics of a tissue ROI
- Normalized response to an instantaneous bolus

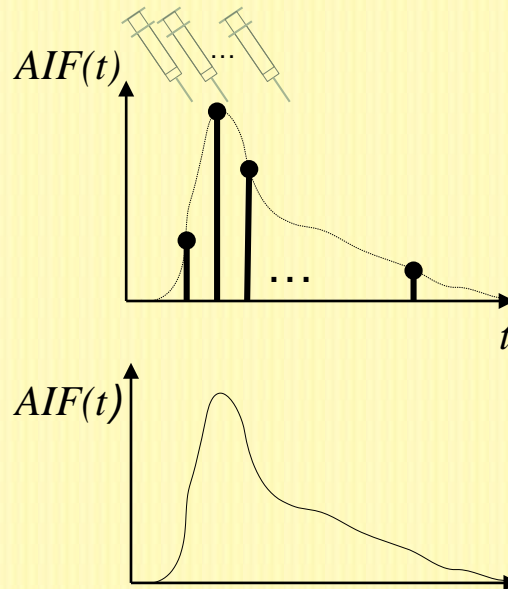


## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

instantaneous  
CA bolus



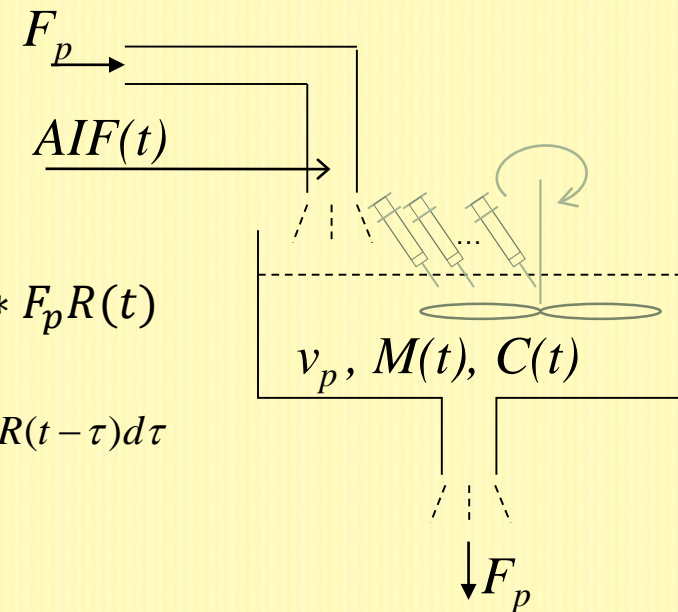
general  
CA bolus



convolution

$$C(t) = AIF(t) * F_p R(t)$$

$$C(t) = F_p \int_0^t AIF(\tau) R(t - \tau) d\tau$$

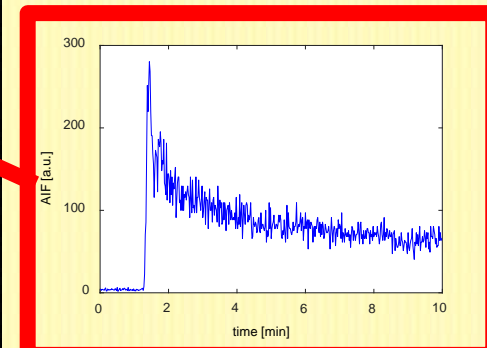
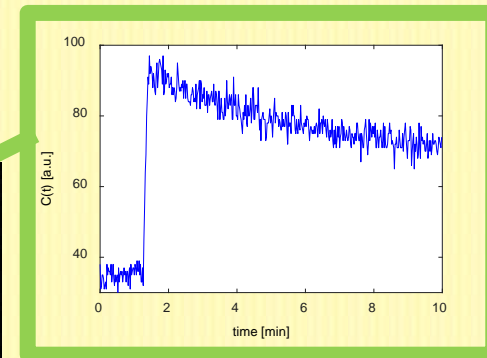


## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

Standard approach:

1. Data acquisition
2. SI  $\rightarrow$   $C(t)$  conversion
3. AIF selection ( $C(t)$  in an artery)
4. Tissue ROI / voxel
5. Deconvolution  $\Rightarrow$  perfusion parameters  
e.g.  $F_p$ ,  $PS$ ,  $v_p$ ,  $v_e$   
( $K^{trans}$ ,  $k_{ep}$ ,  $E$ ,  $T_c$ )

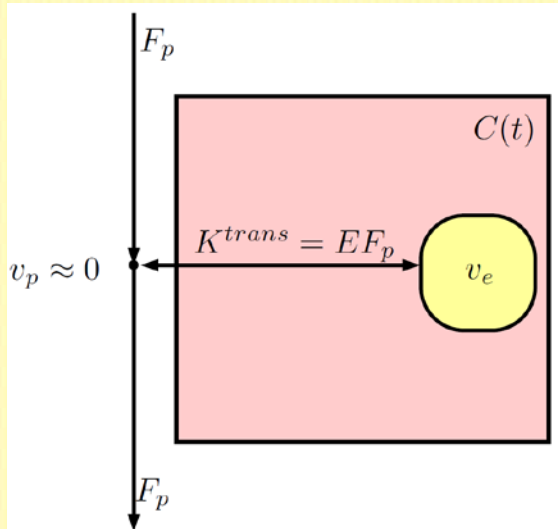
$$C(t) = AIF(t) * F_p R(t)$$



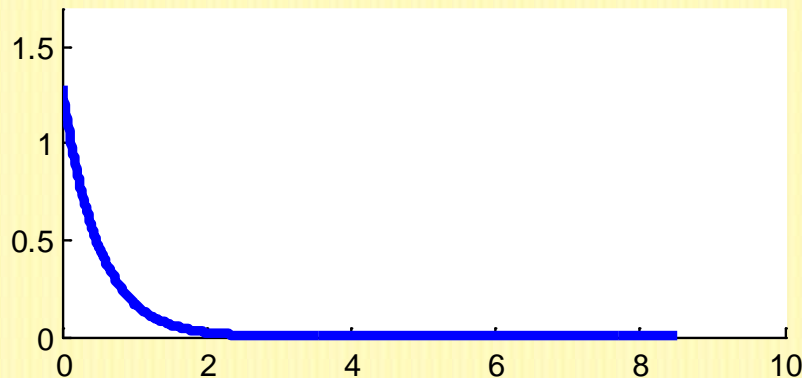
## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

$$C(t) = AIF(t) * F_p R(t)$$

### Tofts

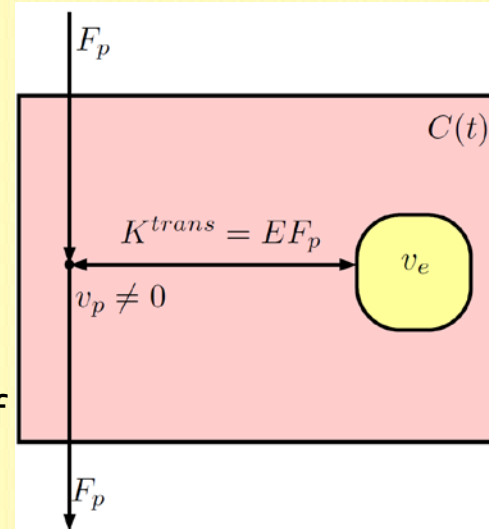


- plasma – neglected
- EES – compartment
- $K^{trans}$ ,  $v_e$  ( $k_{ep} = K^{trans} / v_e$ )
- $K^{trans}$  combination of  $F_p$  and  $PS$

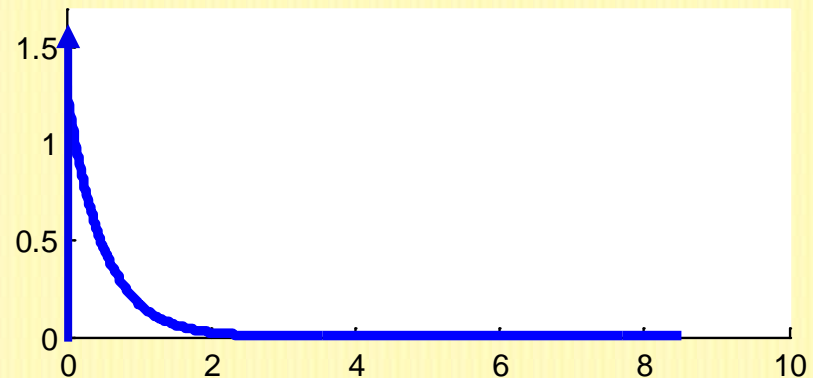


$$C(t) = K^{trans} e^{-k_{ep}t} * c_a(t)$$

### Extended Tofts



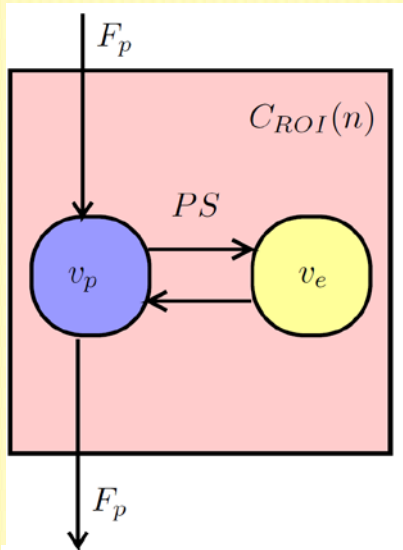
- plasma – equal to AIF
- EES – compartment
- $K^{trans}$ ,  $v_e$ ,  $v_p$  ( $k_{ep} = K^{trans} / v_e$ )
- $K^{trans}$  combination of  $F_p$  and  $PS$



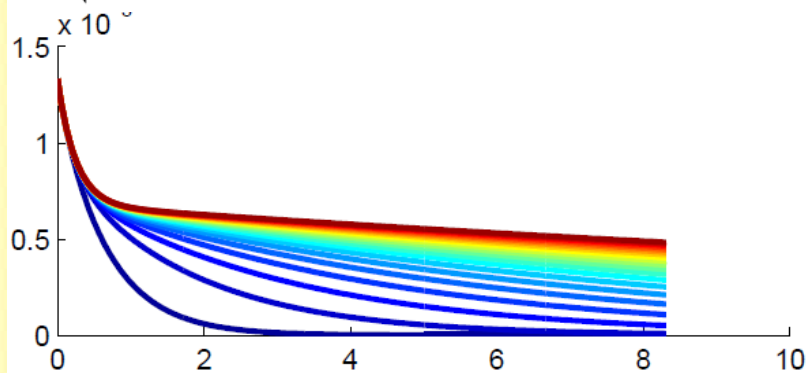
$$C(t) = (v_p \delta(t) + K^{trans} e^{-k_{ep}t}) * c_a(t)$$

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

### 2CXM



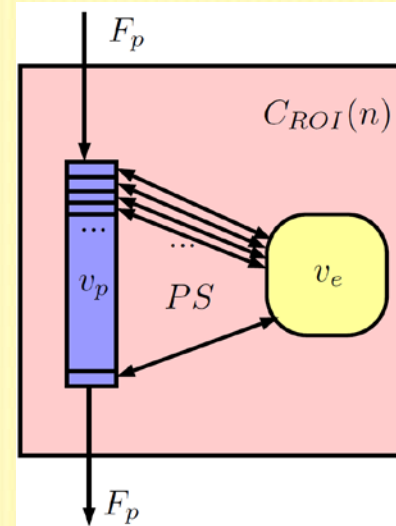
- plasma – compartment
- EES – compartment



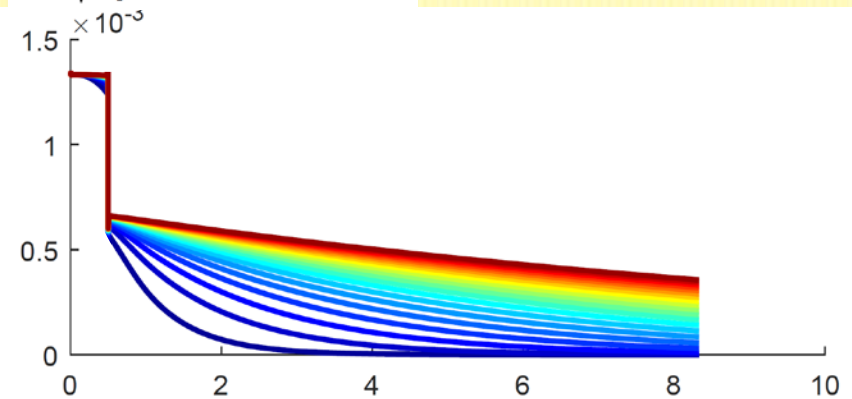
$$C(t) = \frac{(T \alpha_- - 1) \alpha_- e^{-t \alpha_-} + (1 - T \alpha_-) \alpha_+ e^{-t \alpha_+}}{\alpha_+ - \alpha_-} * c_a(t)$$

$$\text{where: } \alpha_{\pm} = \frac{T + T_e \pm \sqrt{(T + T_e)^2 - 4 T_c T_e}}{2 T_c T_e}$$

### TH



- plasma – plug flow
- EES – compartment
- no analytical solution in the time domain

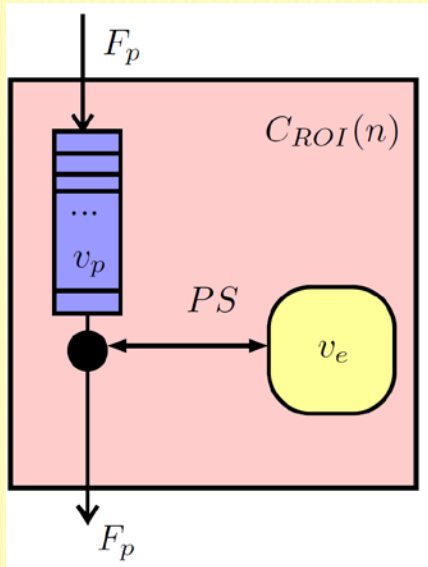


$$h_{TH}(s) = \frac{(T + s T_c T_e)(s T_c + a)(1 - e^{-(s T_c + a)})}{s (T + s T_c T_e)(s T_c + a) + a (1 - e^{-(s T_c + a)})}$$

$$\text{where: } a = \frac{T - T_c}{T_e}$$

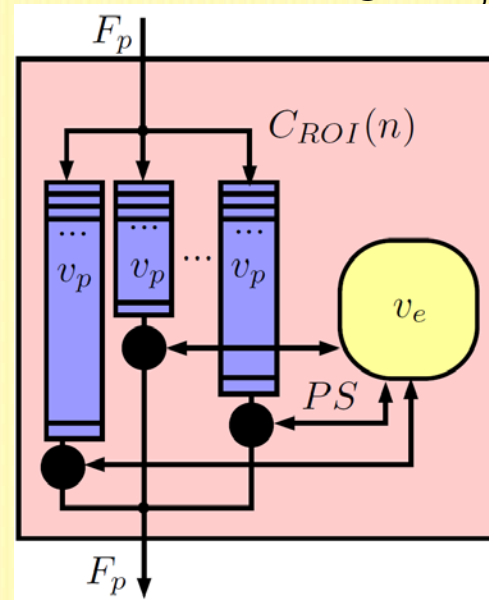
## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

### ATH

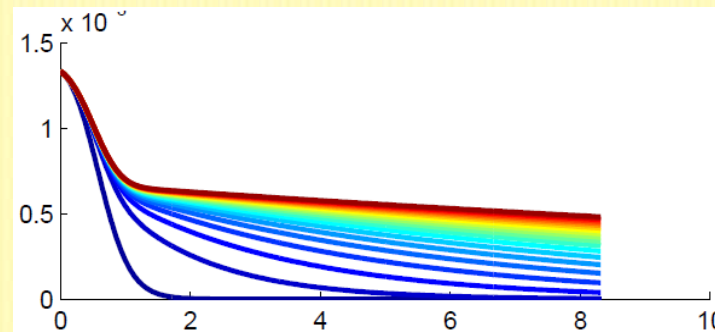
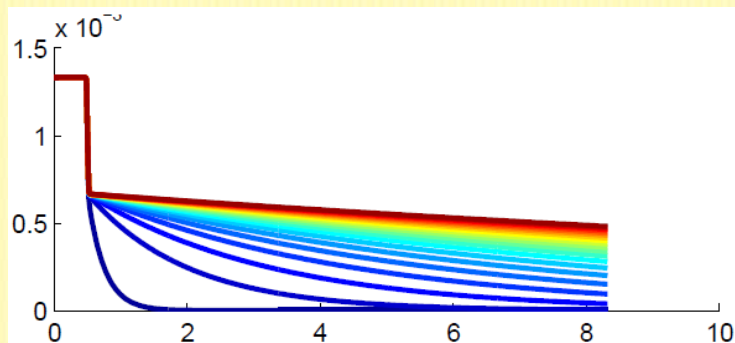


- plasma - plug flow
- EES – compartment
- analytical solution in the time domain
- much slower changes of  $C_e(t)$  than  $C_p(t)$

### DCATH, GCCM



- several capillary paths
- distribution of  $T_c$ :
- DCATH: (truncated) normal, skewed Gaussian
- GCTT: gamma distribution
- additional perf. param.



$$R(\Psi, t) = R_v(\Psi, t) + R_p(\Psi, t),$$

$$R_v(\Psi, t) = 1 - \frac{\text{erf}(\frac{t-\mu}{\sqrt{2}\sigma}) + \text{erf}(\frac{-\mu}{\sqrt{2}\sigma})}{1 + \text{erf}(\frac{\mu}{\sqrt{2}\sigma})}$$

$$R_p(\Psi, t) = \frac{E \exp(\frac{1}{2} k_{ep}^2 \sigma^2 + k_{ep}(\mu - t)) \cdot \text{erf}(\frac{t-\mu}{\sqrt{2}\sigma} - \frac{k_{ep}\sigma}{\sqrt{2}}) + \text{erf}(\frac{-\mu}{\sqrt{2}\sigma} + \frac{k_{ep}\sigma}{\sqrt{2}})}{1 + \text{erf}(\frac{\mu}{\sqrt{2}\sigma})}$$

$$h_{ATH}(t) = F_p \mathcal{H}(T_c - t) + \mathcal{H}(t - T_c) F_p E e^{-\frac{F_p E}{v_e} t} = F_p (R_p(t) + R_e(t))$$

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

$$C(t) = AIF(t) * F_p R(t)$$

IRF model	Perf. farameters	Derived perf. parameters
Tofts	$K^{trans}, v_e$	$k_{ep}$
Extended Tofts	$K^{trans}, v_e, v_p$	$k_{ep}$
2CXM (2CCM)	$F_p, PS, v_p, v_e$	$k_{ep}, K^{trans}$
TH (tissue homogeneity)	$F_p, PS, v_p, v_e$	$k_{ep}, K^{trans}$
ATH (aaTH, aaJW)	$F_p, PS, v_p, v_e$	$k_{ep}, K^{trans}$
DCATH	$F_p, PS, v_p, v_e, \sigma$	$k_{ep}, K^{trans}$
GCTT	$F_p, PS, v_p, v_e, \alpha$	$k_{ep}, K^{trans}$

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

Which of the advanced pharmacokinetic models is more suitable for which application?

### 2CXM

- intravascular space – homogeneous well-mixed space
- for a chaotic spatial arrangement of capillaries, arterioles, venules and larger vascular-tree components

### TH and ATH

- "plug flow" of blood – red blood cells act as "plugs"
- blood plasma between the red blood cells – same velocity
- for parallel vessels of the same length within the ROI

Both simplistic => DCATH and GCTT introduce a statistical distribution of the lengths of the plug-flow capillaries



## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

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Which of the advanced pharmacokinetic models is more suitable for which application?

General requirements

1. realistic
  2. approximation problem should be
    - *well-posed* – unique solution,
    - *well-conditioned* – low sensitivity to noise
- => many vs. few model parameters

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

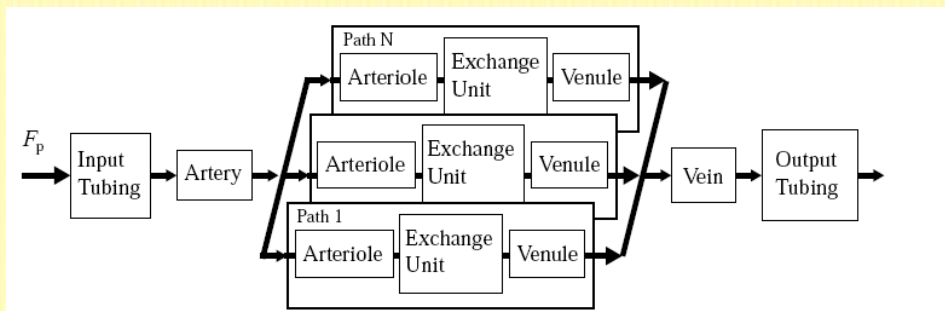
### 1. Choice of a realistic model

No ground truth available

Simulation-based studies

MMID4

- Multiple path, Multiple tracer, Indicator Dilution, 4 region model
- Intravascular, extravascular, intracellular indicators
- partial differential equations
- up to 20 flow paths

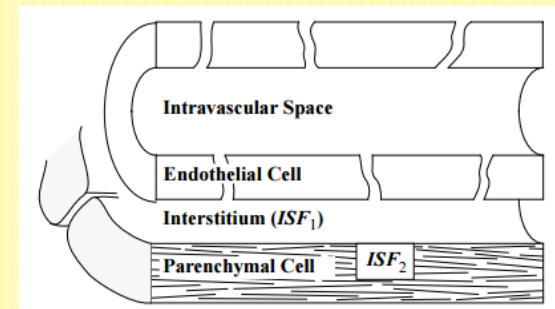


MMID4 model:

<http://physiome.org/jsim/models/webmodel/NSR/MMID4/>

[1] BUCKLEY D. L.. Magnetic Resonance in Medicine 47 (3), 2002, 601–606.

[2] ZHANG J. et al. Magnetic Resonance in Medicine 72 (2), 2014, 534–545.



⇒ Tofts and extended Tofts too simplistic (besides impossible separation of PS and  $F_p$ ) compared to ATH

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

### 1. Choice of a realistic model

#### Real-data based

- quality of models considering their complexity and the goodness of fit
  - Akaike's information criterion (AIC)
  - F-test
- consistency of the estimated perfusion parameters with known assumptions (cervix carcinoma patients)

⇒ Tofts and extended Tofts too simplistic (besides impossible separation of PS and Fp) compared to 2CXM and ATH

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

$$C(t) = AIF(t) * F_p R(t)$$

IRF model	Perf. farameters	Derived perf. parameters
Tofts	$K^{trans}, v_e$	$k_{ep}$
Extended Tofts	$K^{trans}, v_e, v_p$	$k_{ep}$
2CXM (2CCM)	$F_p, PS, v_p, v_e$	$k_{ep}, K^{trans}$
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ATH (aaTH, aaJW)	$F_p, PS, v_p, v_e$	$k_{ep}, K^{trans}$
DCATH	$F_p, PS, v_p, v_e, \sigma$	$k_{ep}, K^{trans}$
GCTT	$F_p, PS, v_p, v_e, \alpha$	$k_{ep}, K^{trans}$

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

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### 2. Choice of a reliable model

Practical experience:

- problems with DCATH, GCTT (5 parameters) for realistic SNR
- 4-parameter models preferable
- 2CXM, ATH
- TH (no analytical solution in the time domain) ???
- DP ???

M. Bartoš et al. *Magn. Reson. Imaging*, 32(5), 2014, 505–13.

M. C. Schabel, *Magn. Reson. Med.*, 68(5), 2012, 1632–1646.

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

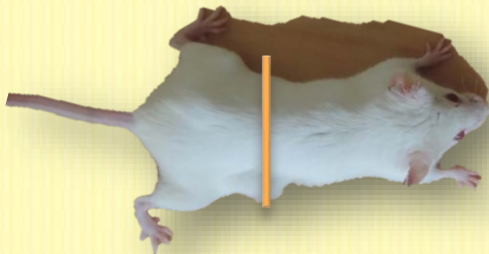
### 2CXM vs. ATH for mouse tumor

high- and low-molecular weight (MW) contrast-agents - consistency with assumed effects of MW:

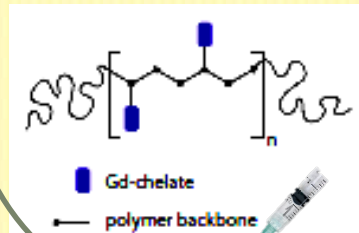
- $F_p$ ,  $v_p$ ,  $T_c$ : MW independent
- $PS$  should decrease with increasing MW

4 BALB/c mice (CT26 tumor)

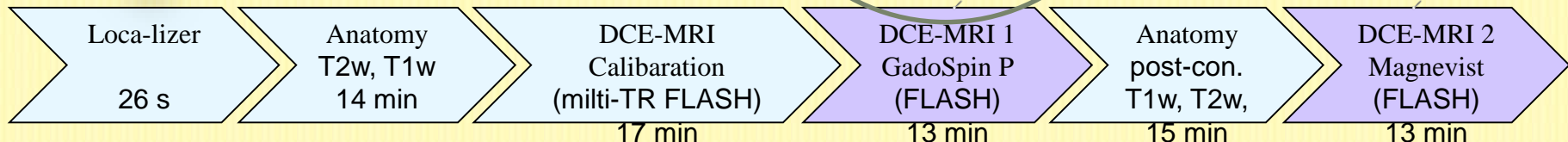
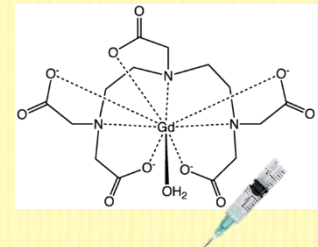
3 hours



GadoSpin P  
200 kDa  
(Miltényi Biotech, Germany)

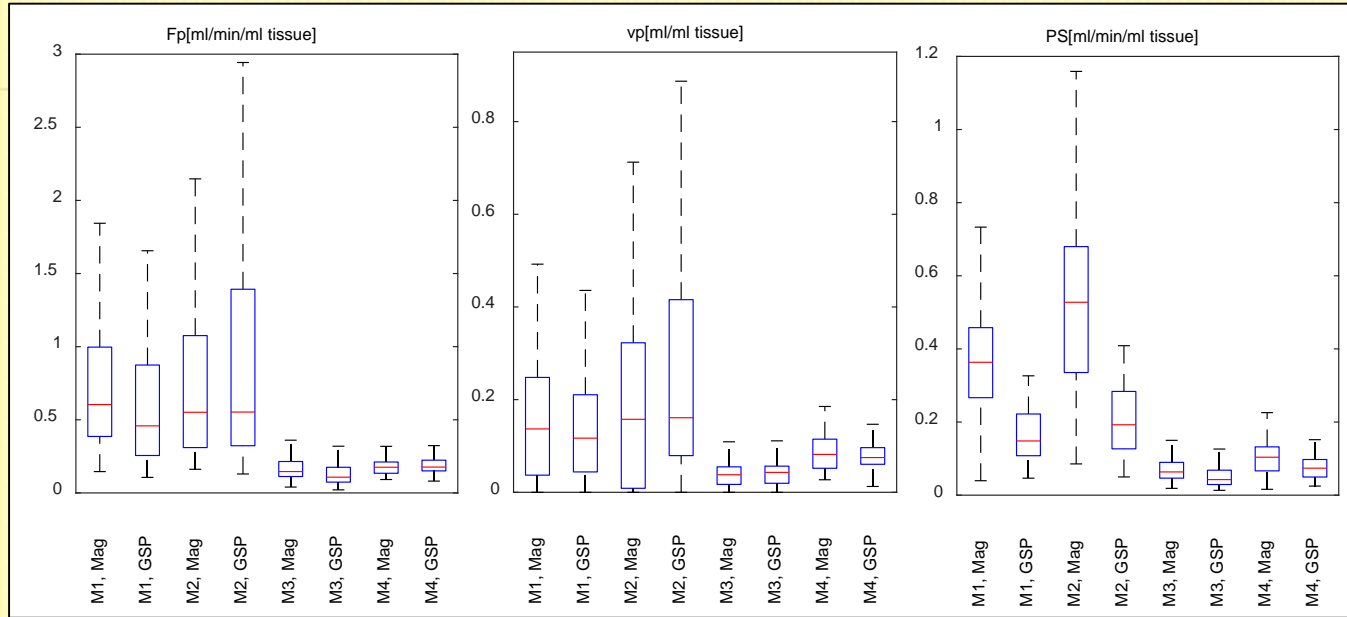


Magnevist  
0.9 kDa  
(Bayer HealthCare, Germany)

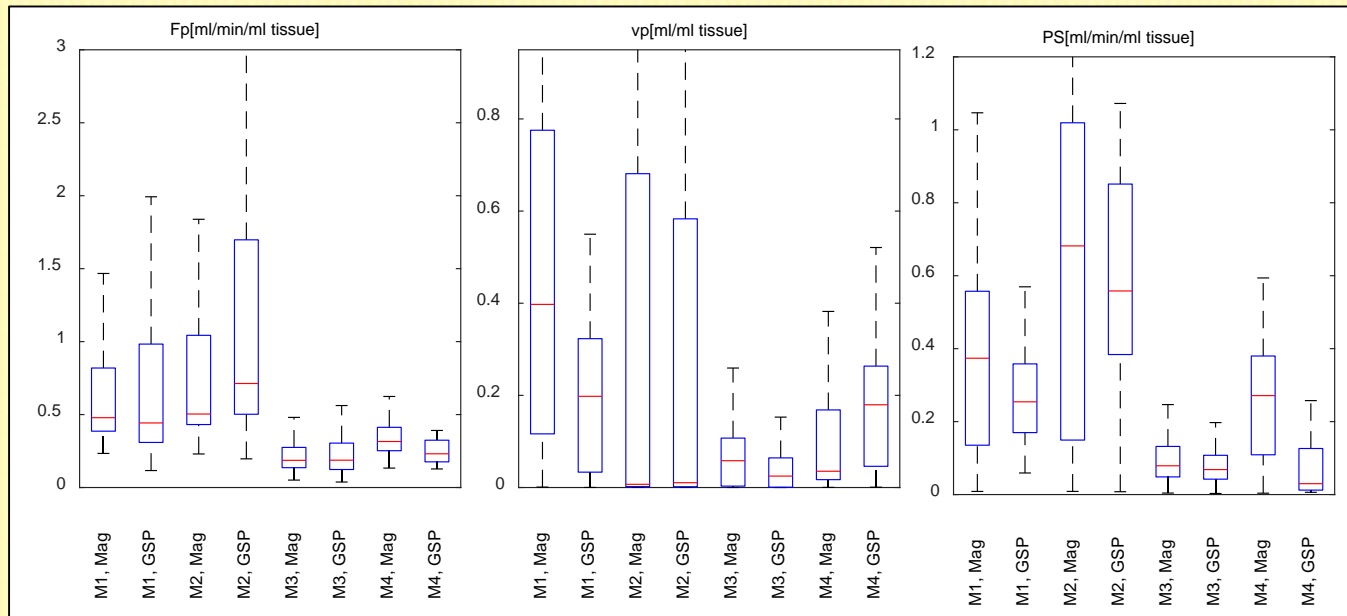


# 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

ATH

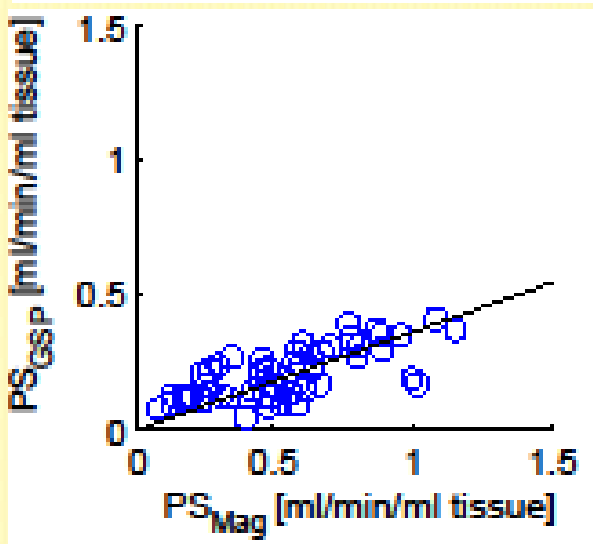
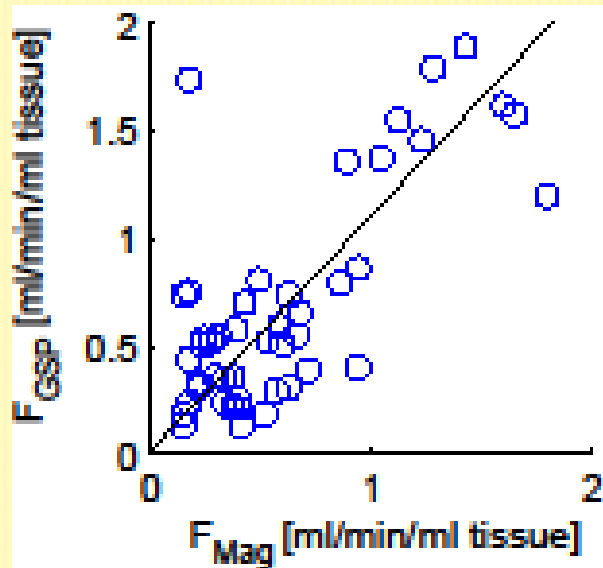


2CXM



⇒ ATH more consistent than 2CXM

## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

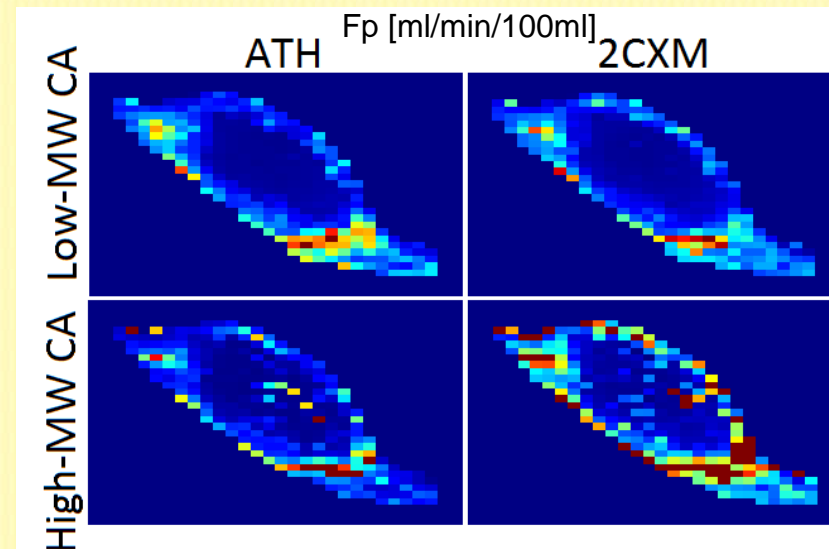


Scatter-plot parameters	AATH		2CXM	
	Mean	SD	Mean	SD
Correlation coef. $F_p$	0.64	0.27	0.54	0.23
Correlation coef. $v_p$	0.72	0.16	0.49	0.32
Correlation coef. PS	0.75	0.12	0.25	0.17
Regression coef., $F_p$	1.20	0.35	1.15	0.16
Regression coef., $v_p$	0.98	0.27	0.43	0.30
Regression coef., PS	0.43	0.21	0.57	0.22

⇒ ATH better than 2CXM

- better optimization conditioning
- and/or more realistic (even though both are still simplistic)

difference not clear in visual assessment of perfusion maps:





## 2. PERFUSION IMAGING – PHARMACOKINETIC MODELING

Comparison of

- 2CXM, ATH (aaTH) (4 parameters)
- DCATH, GCTT (5 parameters)

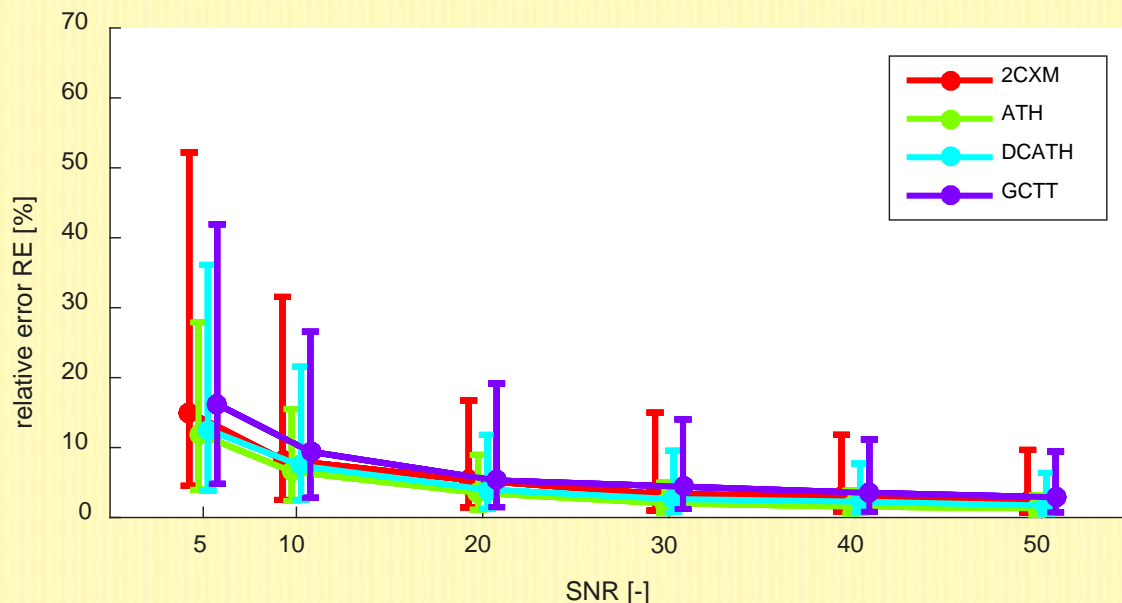
in terms of conditioning of the deconvolution problem

Synthetic data

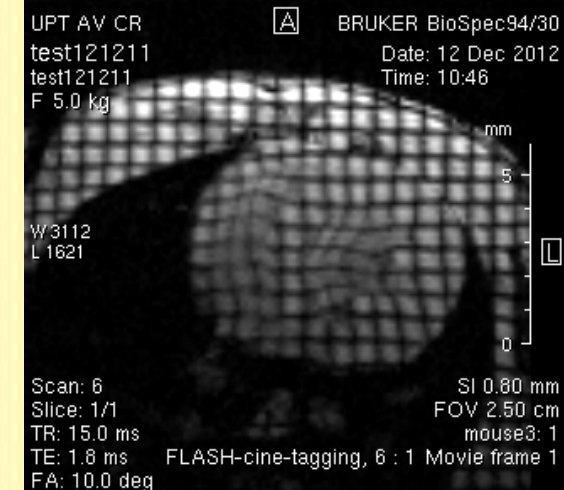
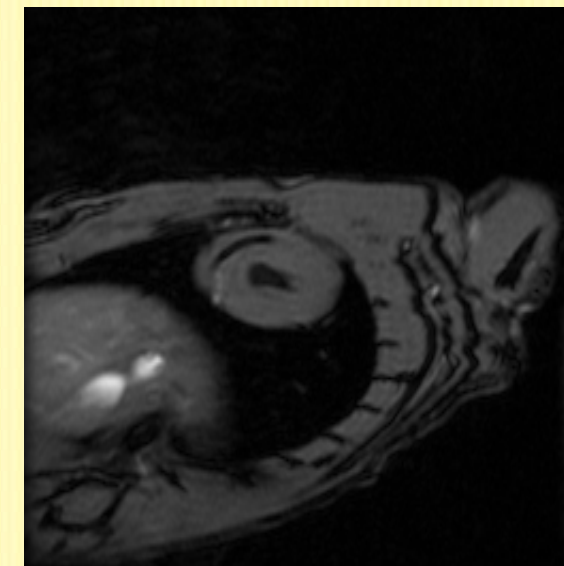
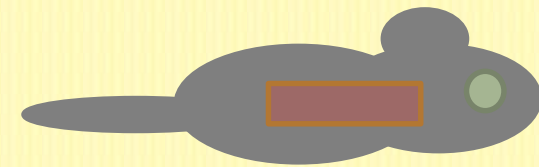
- the same model used for data generation and deconvolution
- 3 tissues (glioblastoma, prostate and colorectal tumor)
- 100 noise realizations per tissue

- median and 25%, 75% percentiles of relative estim. error of  $F_p$ ,  $T_c$ ,  $E$ ,  $v_e$ ,  $BAT$ ,  $\alpha^{-1}$ ,  $\sigma$

2CXM the worst  
ATH the best



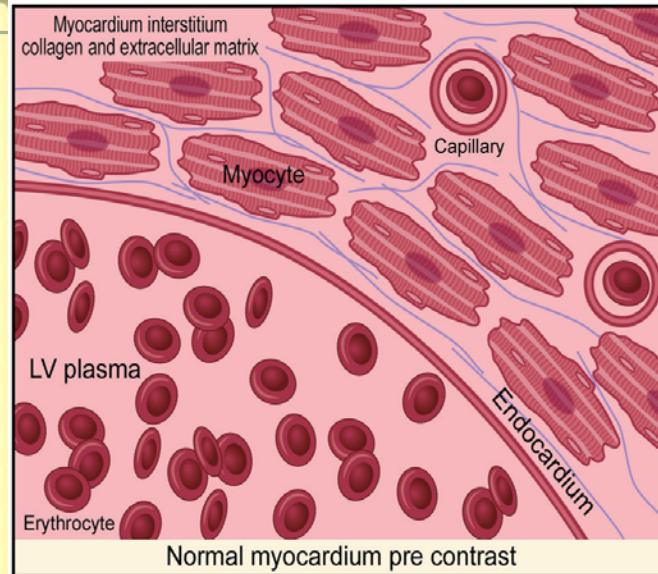
# 3. T1 QUANTIFICATION - MYOCARDIUM



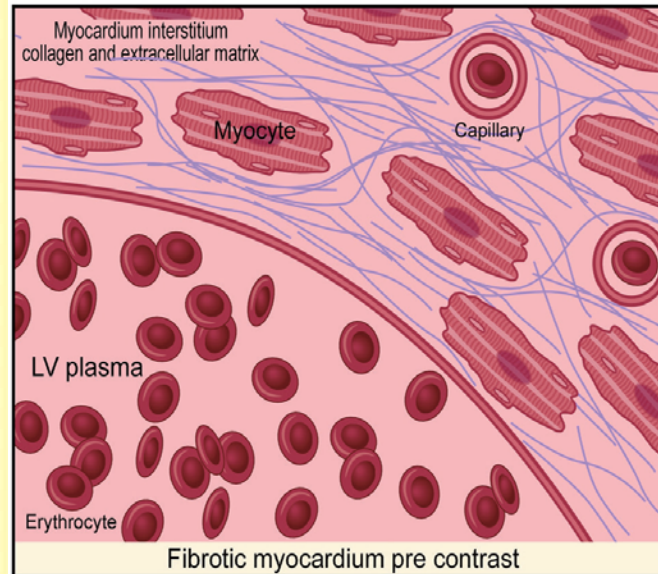
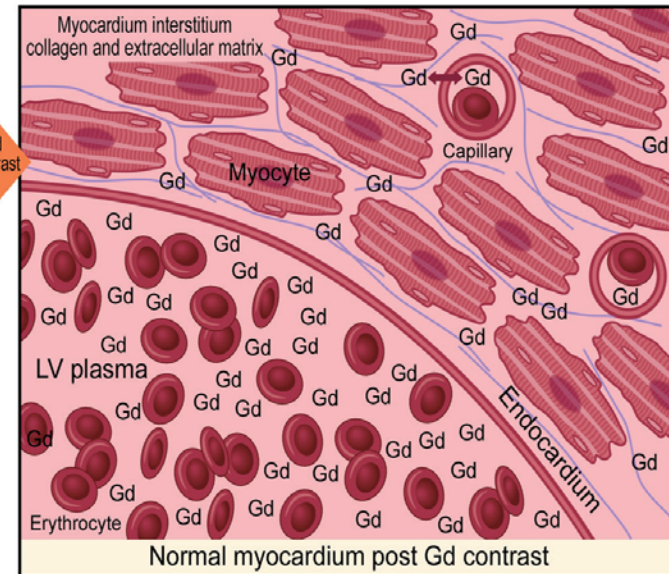
### 3. T1 QUANTIFICATION

Quantification  
of fibrosis

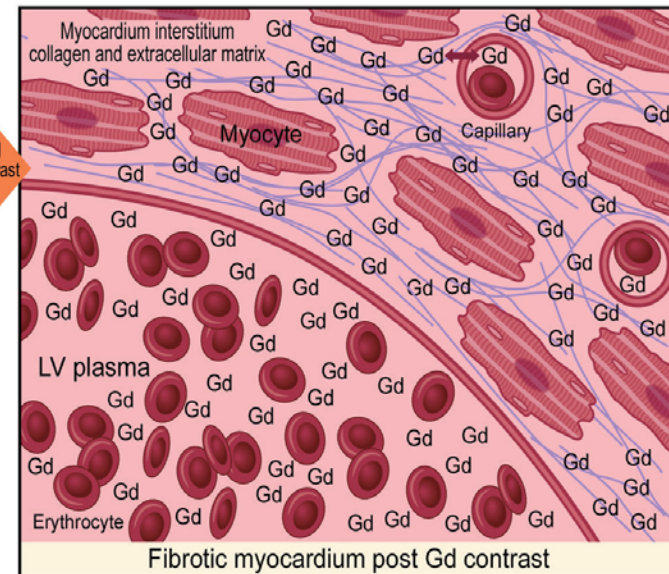
- ✖ Focal  
(myocardial  
infarction)
- ✖ Diffusive  
(dilated  
cardiomyopathy)



Gd Contrast



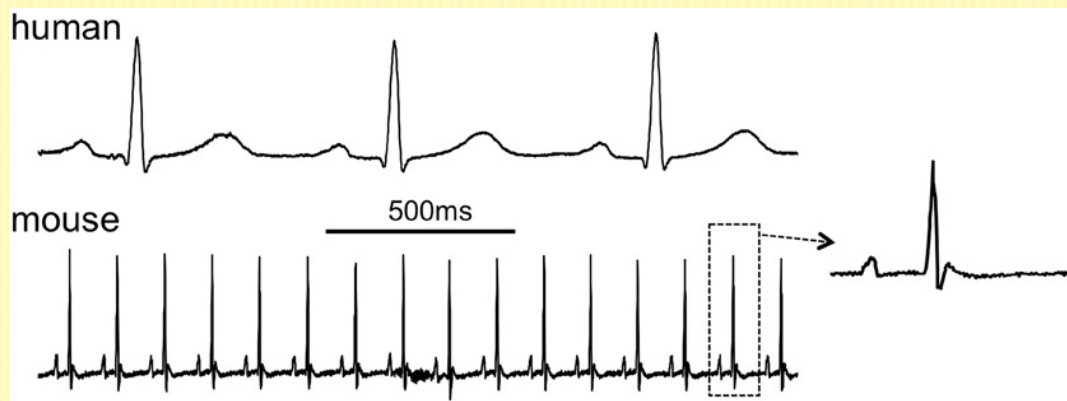
Gd Contrast



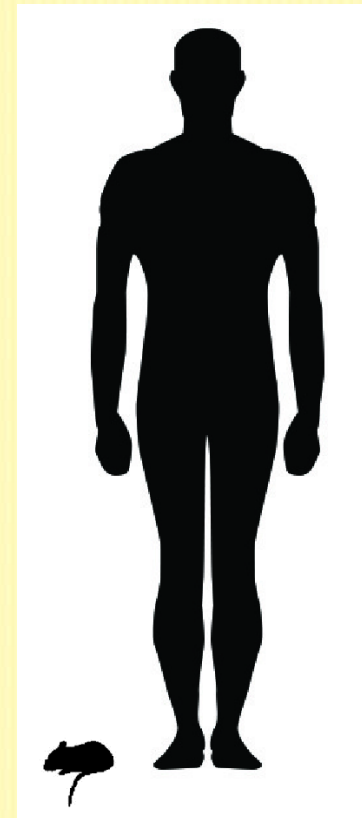


### 3. T1 QUANTIFICATION

- Small animal model
  - Smaller size of the heart
  - Faster ECG and respiration rates
  - rat: 350 BPM, 40-60 1/min
  - (mouse: 450 BMP, 50-80 1/min)
  - in anesthesia
  - no breathhold acquisition possible



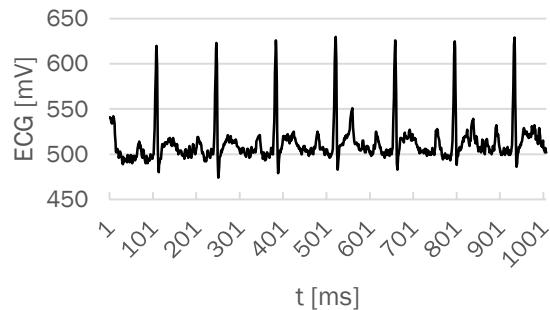
Kease, Front. Physiol, 2012



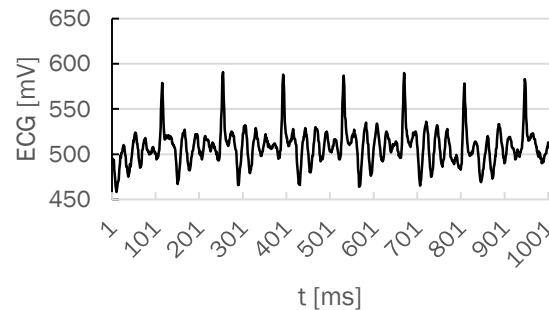
# 3. T1 QUANTIFICATION

## ECG triggering

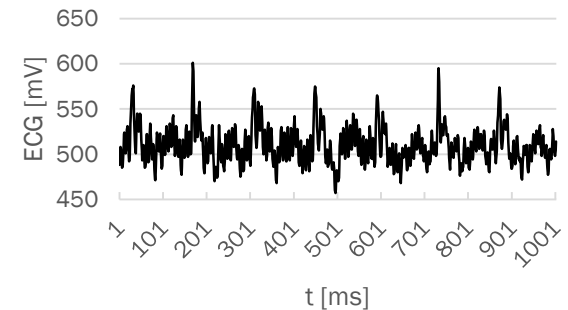
- needle subcutaneous ECG electrodes



ECG of rat, outside the magnetic field



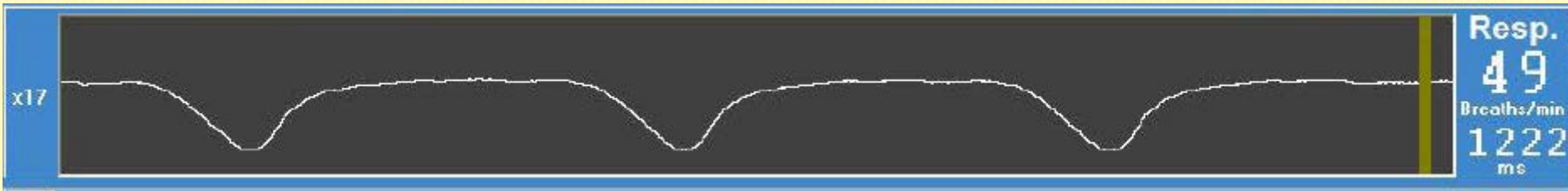
ECG of rat, inside the magnetic field



ECG of rat, during the data acquisition

## Respiration triggering

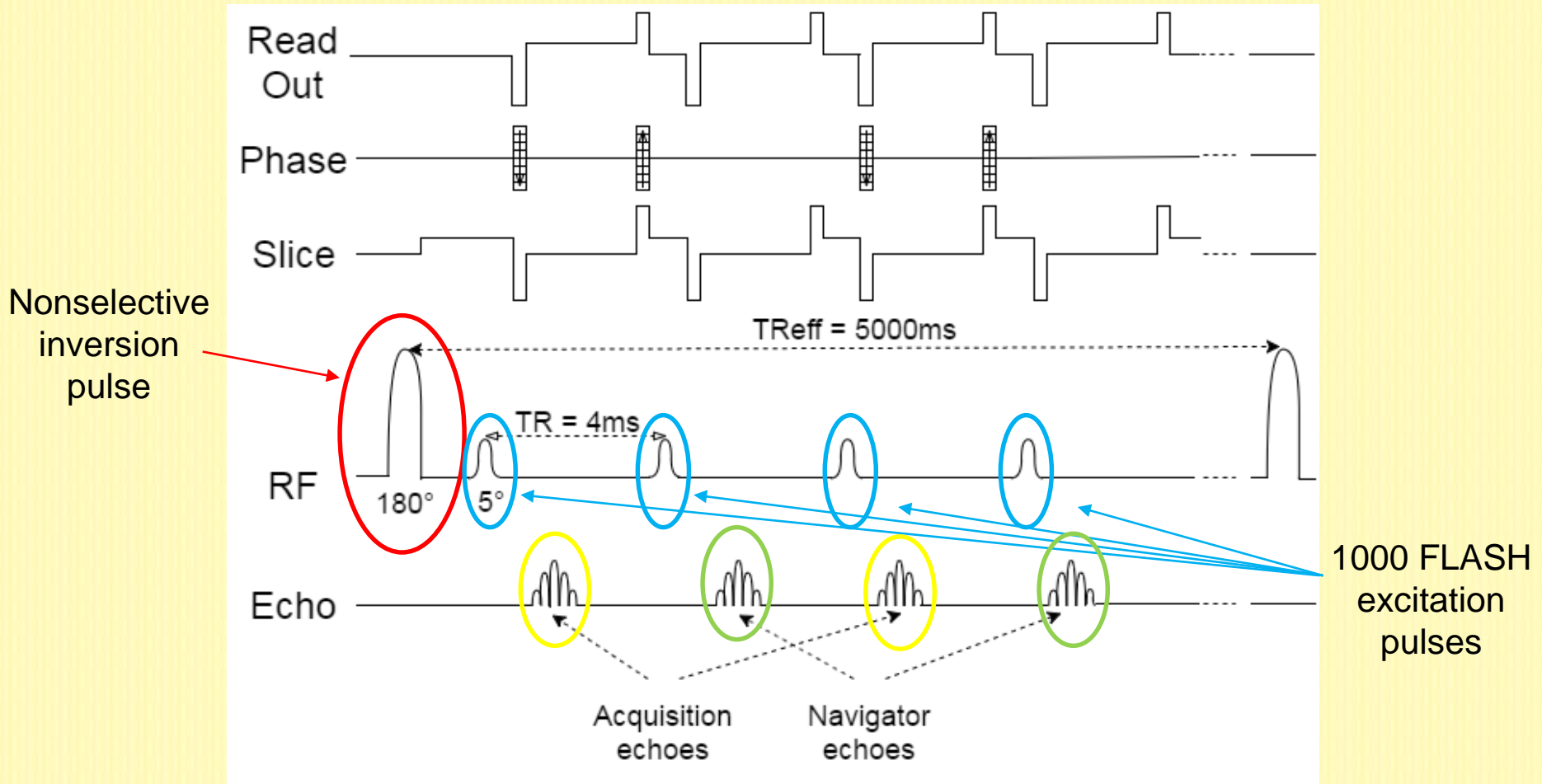
- respiration pillow



### 3. T1 QUANTIFICATION

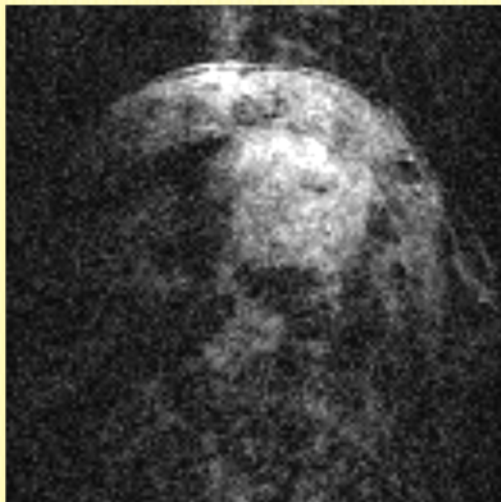
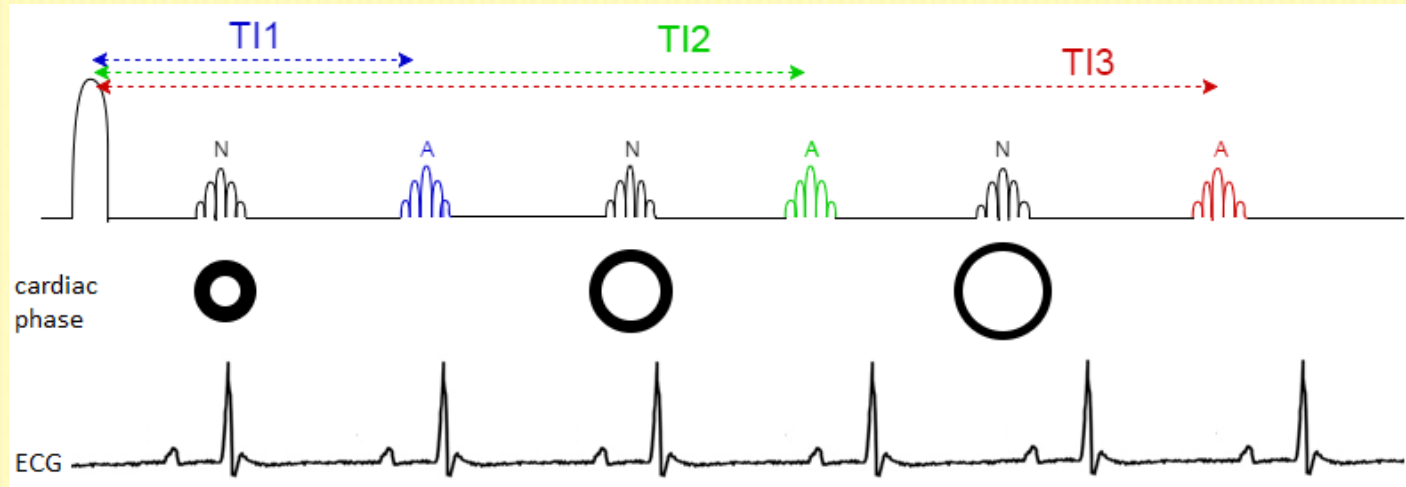
#### Retrospective gating

- no measuring of ECG and respiration, navigators



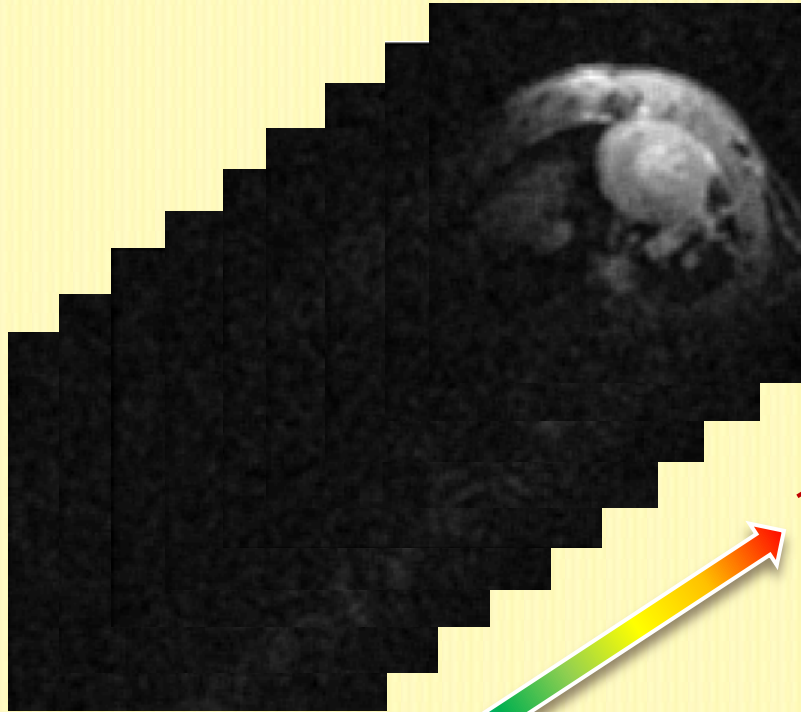
### 3. T1 QUANTIFICATION

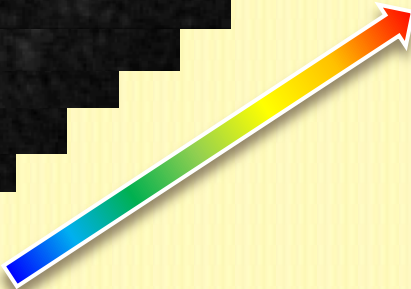
Image reconstruction



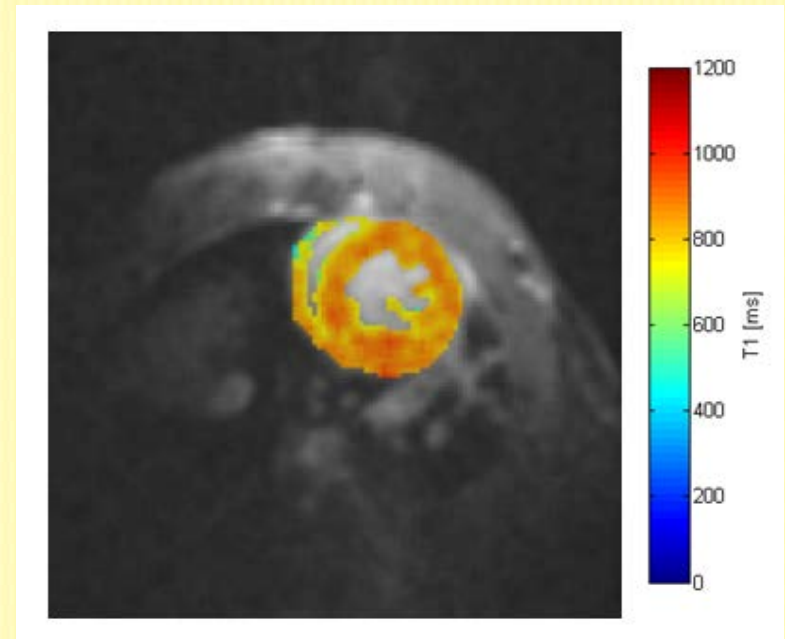
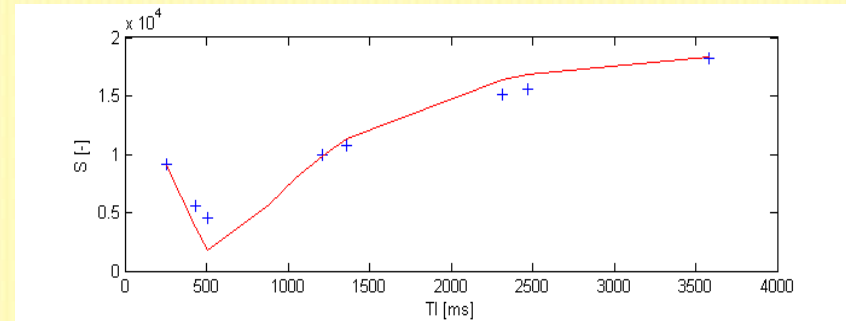
### 3. T1 QUANTIFICATION

Image reconstruction



TI min  TI max

$$S = |S_0(1 - 2e^{-\frac{TI}{T_1}})|$$





### 3. T1 QUANTIFICATION

Doxorubicin

chemotherapy



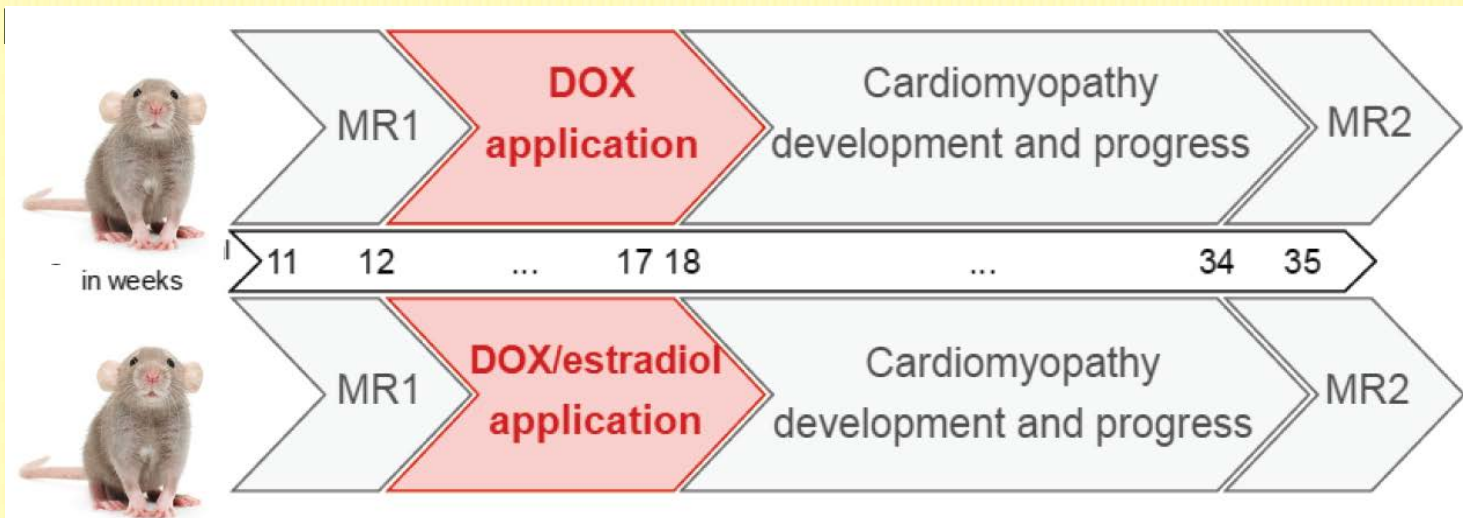
model of dilated cardiomyopathy



### 3. T1 QUANTIFICATION

#### Doxorubicin study

- 18 rats (9 rats survived)
  - 9 doxorubicin treatment (5 survived)
  - 9 doxorubicin + estradiol (hormone-probably increases doxorubicin cardiotoxicity) treatment (4 survived)
- 2 examinations
  - Baseline
  - 18 weeks after treatment
- Anatomical imaging (ejection fraction)



### 3. T1 QUANTIFICATION

## Dilated cardiomyopathy

### Fibrosis:

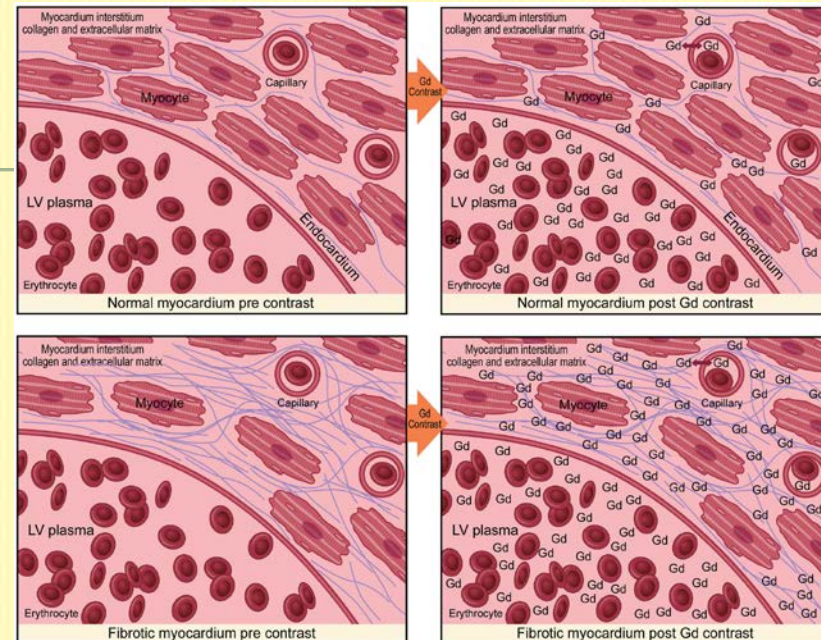
- Higher pre-contrast T1
- Lower post-contrast T1
- Lower ejection fraction

## Results

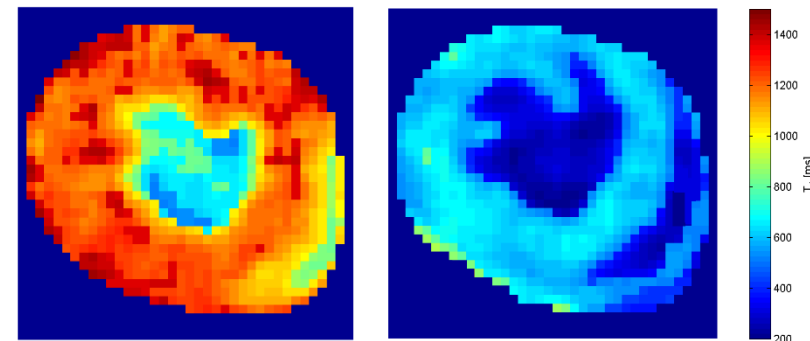
Results of statistical analysis for measurements pre versus post treatment

	DOX/ estradiol	DOX	
native T1	↑	↑*	⇒ fibrotic tissue in myocardium
post-contrast T1	↓*	↑	⇒ fibrotic tissue in myocardium (in DOX/estradiol group)
LVEF	↓*	↓*	⇒ cardiotoxicity of both DOX and estradiol confirmed

\* indicates a statistical significant result



Jellis, Kwon, Cardiovascular Imaging, 2013

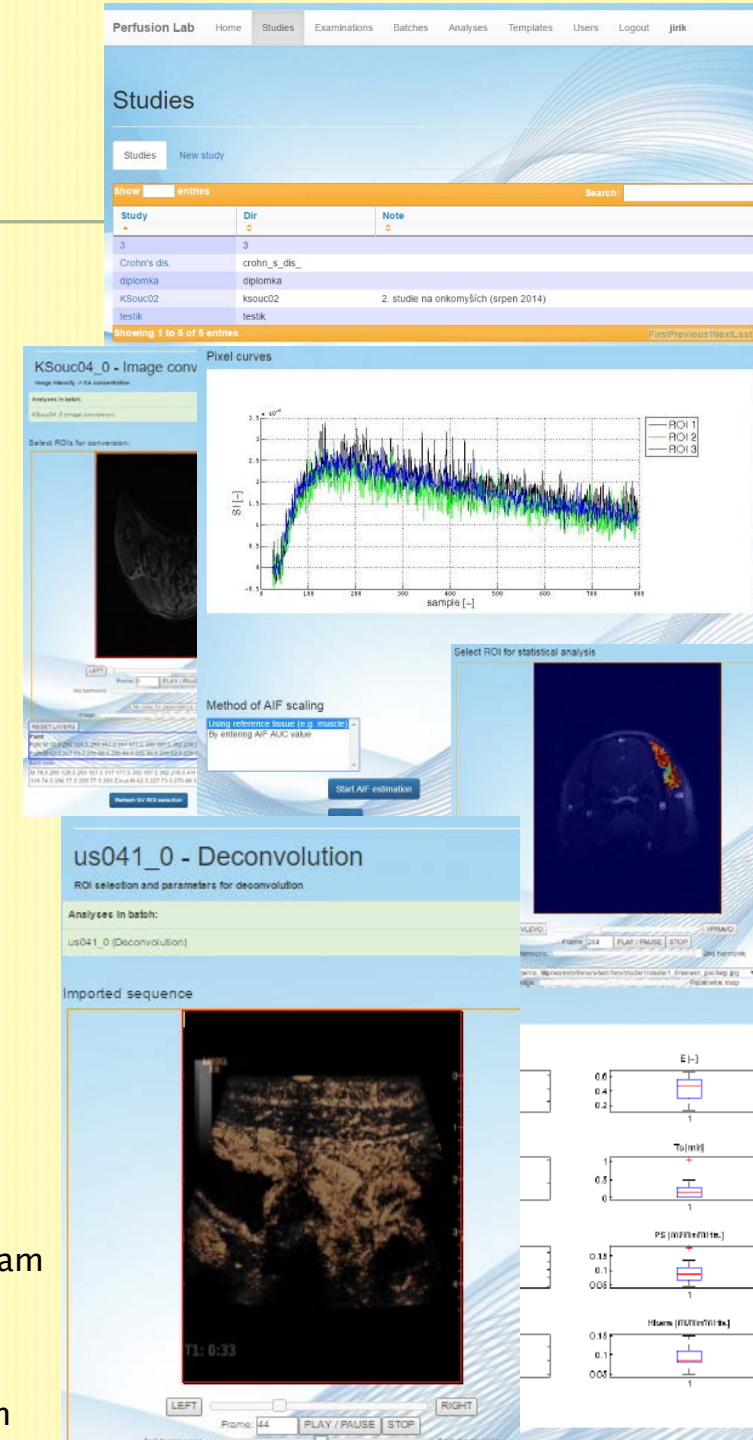


Pre-contrast T1 map Post-contrast T1 map

# CONCLUSIONS

## qMRI

- comparability of the data generated at different sites and time points and using different scanners
- assumptions of models
- underlying models have to be realistic and lead to well-posed and well-conditioned approximation
- animal studies – alternative ways of validation



<http://perflab.cerit-sc.cz/>

## DCE-MRI

- Blind deconvolution (so far preclinical AIF)
- ATH, 2CXM, Tofts, ext. Tofts pharmacokinetic models
- ...more will come soon

## DCE-US

- Bolus&burst
- AIF models: 2gam, 3gam
- Automatic image registration
- So far – single regions
- ...more will come soon



# THANK YOU FOR YOUR ATTENTION!

